

## 1 Multicollinearity

What is multicollinearity (MC)?

- Multicollinearity is multivariate correlation amongst the explanatory variables
  - Perfect MC: Violates a classical assumption & OLS can't be calculated
  - Imperfect MC: Typical case, no violation of classical assumptions

**Consequences (of imperfect MC)**

- OLS is still B.L.U.E.
- Estimates can be unreliable and imprecise
- High standard errors
- Low  $t$  statistics
- Can still have high  $R^2$  value

**Detection**

- Low  $t$  statistics & high  $R^2$  value
- Pairwise correlations:  $-1 \leq r_{ij} \leq 1$ 
  - Rule of thumb:  $abs(r_{ij}) > 0.8 \implies$  severe MC
  - Sufficient condition
- Variance inflation factors:  $VIF(\hat{\beta}_j) = (1 - R_j^2)^{-1}$ 
  - Rule of thumb:  $VIF(\hat{\beta}_j) > 5 \implies$  severe MC
  - Necessary and sufficient condition

**Solutions**

- Do nothing
- Get a larger sample
- Transform variables (e.g., ratios, first-differences, etc.)

- Drop a variable

### **Application**

- Earnings regression